

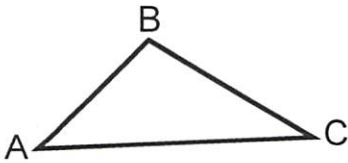
H.W pf 348 14-22
 pf 367 7-17 odd #21

5.5 Inequalities in one Triangle

5.3 Angle Side Relationships in Triangles

Objective: To use the triangle inequality theorem to identify possible triangles
 To recognize and apply properties of inequalities to the relationships between the angles and sides of a triangle

Triangle Inequality Theorem: The sum of any two sides of a triangle must be greater than the 3rd side.



$$\begin{aligned} AB + BC &> AC \\ BC + AC &> AB \\ AC + AB &> BC \end{aligned}$$

1. Is it possible to have a triangle with the following 3 side lengths?

- a) 5, 2, 4 $2+4 > 5$ yes, $5+2 > 4$, $5+4 > 2$
 b) 5, 2, 3 $2+3 > 5$ NO
 c) 5, 2, 2 $2+2 > 5$ NO
 d) 5, 2, 5 $2+5 > 7$ yes

2. Write an inequality statement to represent the range of possible lengths for the 3rd side of a triangle(x).

a) 3 and 5

$$\begin{aligned} x+3 &> 5, & x+5 &> 3, & 3+5 &> x \\ x &> 2, & x &> -2, & 8 &> x \end{aligned}$$

$2 < x < 8$ $8 > x$ or $x < 8$

* 8 and 11

$$\begin{aligned} x+8 &> 11, & x+11 &> 8, & 8+11 &> x \\ x &> 3, & x &> -3, & 19 &> x \end{aligned}$$

$3 < x < 19$

b) k and k + 8

$$\begin{aligned} x+k &> k+8, & x+k+8 &> k, & k+8+k &> x \\ x &> 8, & x &> -8, & 2k+8 &> x \end{aligned}$$

$8 < x < 2k+8$

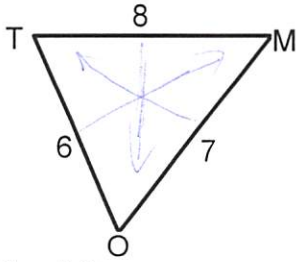
you try: k and k + 10

$$\begin{aligned} x+k+10 &> k, & x+k &> k+10, & k+k+10 &> x \\ x &> -10, & x &> 10, & 2k+10 &> x \end{aligned}$$

$10 < x < 2k+10$
 $10 < x < 2k+10$

Section 5.3 (Theorems on pg. 346)

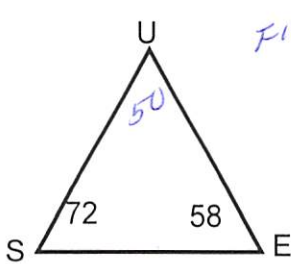
Theorem 5.9: In a triangle, if one side is longer than another side then the bigger angle will be across from the longer side.



observe: $TO < OM < TM$
conclude: $\angle M < \angle T < \angle O$

Section 5.3

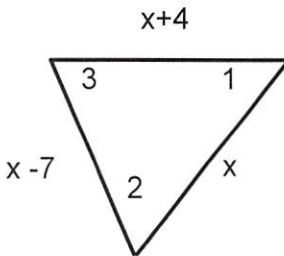
Theorem 5.10: In a triangle, if one angle is larger than another angle, then the longer side will be across from the bigger angle.



observe: $\angle U < \angle E < \angle S$
conclude: $SE < SU < UE$

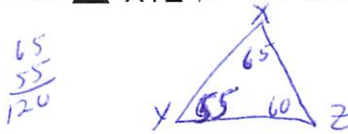
Practice:

3. Name the largest angle:



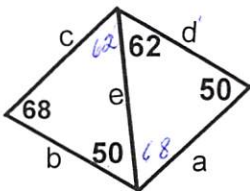
it is opposite the longest side
 $\angle 2$

4. In $\triangle XYZ$, $x = 65^\circ$ and $y = 55^\circ$ Name the shortest side.

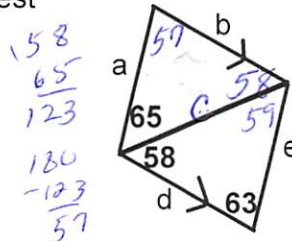


$\angle Z$ is smallest since it's opposite smallest angle

5. Write lengths a,b,c,d,e from smallest to largest



$\frac{62}{112}$



$\frac{158}{123}$
 $\frac{180}{57}$

$\frac{58}{121}$
 $\frac{63}{59}$

$c < b < e$
 $e < a < d$

$\angle A < \angle B$
 $\angle D < \angle C$

ANSWER
 $e < d < c < a < b$

ANSWER: $c < b < e < a < d$

y time
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